

## CLAIMS

I claim:

1. A method of removing empty string terms from an automaton A having a set of states "p", a set of states "q", and a set of outgoing transitions from the set of states "p", E[p], the method comprising:

computing an  $\epsilon$ -closure for each state "p" of the automaton A;

modifying E[p] by:

removing each transition labeled with an empty string; and

adding to E[p] a non-empty-string transition, wherein each state "q" is left with its weights pre-multiplied by an  $\epsilon$ -distance from state "p" to a state "q" in the automaton A.

2. The method of claim 1, further comprising:

removing inaccessible states using a depth-first search of the automaton A.

3. The method of claim 1, wherein adding to E[p] non-empty-string transitions further comprises leaving q with weights  $(d[p,q] \otimes \rho[q])$  to E[p].

4. The method of claim 1, wherein the step of computing  $\epsilon$ -closure for each input state of an input automaton A further comprises:

removing all transitions not labeled with an empty string from automaton A to produce an automaton  $A_\epsilon$ ;

decomposing  $A_\epsilon$  into its strongly connected components; and

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computing all-pairs shortest distances in each component visited in reverse topological order.

5. The method of claim 1, wherein the step of computing  $\varepsilon$ -closure for each input state of an input automaton A further comprises:

decomposing  $A_\varepsilon$  into its strongly connected components;

performing a single-source shortest-distance algorithm according to the following pseudo code:

```
1 for each  $p \in Q$ 
2   do  $d[p] \leftarrow r[p] \leftarrow \bar{O}$ 
3  $d[s] \leftarrow r[s] \leftarrow \bar{1}$ 
4  $S \leftarrow \{s\}$ 
5 while  $S \neq \emptyset$ 
6   do  $q \leftarrow \text{head}[S]$ 
7   DEQUEUE(S)
8    $r \leftarrow r[q]$ 
9    $r[q] \leftarrow \bar{O}$ 
10  for each  $e \in E[q]$ 
11    do if  $d[n[e]] \neq d[n[e]] \oplus (r \otimes w[e])$ 
12      then  $d[n[e]] \leftarrow d[n[e]] \oplus (r \otimes w[e])$ 
13       $r[n[e]] \leftarrow r[n[e]] \oplus (r \otimes w[e])$ 
14      if  $n[e] \notin S$ 
15        then ENQUEUE(S,  $n[e]$ )
16  $d[s] \leftarrow \bar{1}$ 
```

6. The method of claim 1, wherein the step of computing the  $\varepsilon$ -closure for each state "p" further comprises computing each the  $\varepsilon$ -closure according to the following equation:

$$C[p] = \{(q, w) : q \in c[p], d[p, q] = w \in K - \{\bar{O}\}\}.$$

7. The method of claim 6, wherein the step of modifying outgoing transitions of each state "p" further comprises modifying the outgoing transitions of each state p according to the following procedure:

- (1) **for each**  $p \in Q$
- (2)     **do**  $E[p] \leftarrow \{e \in E[p] : i[e] \neq \epsilon\}$
- (3)     **for each**  $(q, w) \in C[p]$
- (4)         **do**  $E[p] \leftarrow E[p] \cup \{(p, a, w \otimes w', r) : (q, a, w', r) \in E[q], a \neq \epsilon\}$
- (5)         **if**  $q \in F$
- (6)             **then if**  $p \notin F$
- (7)                 **then**  $F \leftarrow F \cup \{p\}$
- (8)                  $\rho[p] \leftarrow \rho[p] \oplus (\omega \oplus \rho[q])$

8. The method of claim 7, wherein a state is a final state if some state “q” within a set of states reachable from “p” via a path labeled with an empty string is final and the final weight is then:  $\rho[p] = \bigoplus_{q \in e[p] \cap F} (d[p, q] \otimes \rho[q])$ .

9. The method of claim 8, further comprising:

performing a depth-first search of the automaton A after removing the empty strings.

10. A method of producing an equivalent weighted automaton “B” with no  $\epsilon$ -transitions for any input weighted automaton “A” having at least one  $\epsilon$ -transition, the automaton “A” having a set of states “p”, and a set of states “q”, the method comprising:

computing an  $\epsilon$ -closure for each state “p” of the input weighted automaton “A”;

modifying outgoing transitions of each state “p” by:

removing each transition labeled with an empty string; and

adding to each transition leaving state “p” a non-empty-string

transition, wherein each state “q” is left with its weights pre-multiplied by an

$\epsilon$ -distance from state “p” to “q” in the automaton “A” to produce the automaton “B” equivalent to automaton A without the  $\epsilon$ -transitions.

11. The method of claim 10, further comprising:  
removing inaccessible states using a depth-first search of the automaton.
12. The method of claim 11, wherein adding to the outgoing transitions non-empty-string transitions further comprises leaving each state “q” with weights  $(d[p, q] \otimes \rho[q])$  to the transitions leaving p.
13. A method of claim 10, wherein the step of computing an  $\epsilon$ -closure for each input state of an input automaton “A” further comprises:  
removing all non- $\epsilon$ -transitions to produce an automaton  $A_\epsilon$ ;  
decomposing  $A_\epsilon$  into its strongly connected components; and  
computing all-pairs shortest distances in each component visited in reverse topological order.
14. The method of claim 10, wherein the step of computing the  $\epsilon$ -closure for each state “p” further comprises computing each of the  $\epsilon$ -closures according to the following equation:
$$C[p] = \{(q, w) : q \in \epsilon[p], d[p, q] = w \in K - \{\bar{O}\}\}.$$
15. The method of claim 14, wherein the step of modifying outgoing transitions of each state “p” further comprises modifying the outgoing transitions of each state p according to the following procedure:

- (1) **for** each  $p \in Q$
- (2)     do  $E[p] \leftarrow \{e \in E[p] : i[e] \neq \epsilon\}$
- (3)     **for** each  $(q, w) \in C[p]$
- (4)         do  $E[p] \leftarrow E[p] \cup \{(p, a, w \otimes w', r) : (q, a, w', r) \in E[q], a \neq \epsilon\}$
- (5)         **if**  $q \in F$
- (6)             **then if**  $p \notin F$
- (7)                 **then**  $F \leftarrow F \cup \{p\}$
- (8)                  $\rho[p] \leftarrow p[p] \oplus (\omega \oplus \rho[q])$ .

16. A method of producing an automaton B from an automaton A, the automaton B having no empty string transitions, the method comprising:

computing for each state p in automaton A its  $\epsilon$ -closure  $C[p]$  according to the following:  $C[p] = \{(q, w) : q \in \epsilon[p], d[p, q] = w \in K - \{\bar{O}\}\}$ , where  $\epsilon[p]$  represents states labeled with an empty string;

removing each transition labeled with an empty string; and

adding to each transition leaving state “p” a non-empty-string transition, wherein each state “q” is left with its weights pre-multiplied by an  $\epsilon$ -distance from state “p” to “q” in the automaton “A” to produce the automaton “B” equivalent to automaton A without the  $\epsilon$ -transitions.

17. The method of claim 16, wherein adding non-empty strings to  $E[p]$  is performed according to the following code:

- (1) **for** each  $p \in Q$
- (2)     do  $E[p] \leftarrow \{e \in E[p] : i[e] \neq \epsilon\}$
- (3)     **for** each  $(q, w) \in C[p]$
- (4)         do  $E[p] \leftarrow E[p] \cup \{(p, a, w \otimes w', r) : (q, a, w', r) \in E[q], a \neq \epsilon\}$
- (5)         **if**  $q \in F$
- (6)             **then if**  $p \notin F$
- (7)                 **then**  $F \leftarrow F \cup \{p\}$
- (8)                  $\rho[p] \leftarrow p[p] \oplus (\omega \oplus \rho[q])$ ,

18. The method of claim 10, further comprising modifying  $E[p]$  according to the following procedure:

- (1) **for each**  $p \in Q$
- (2)     do  $E[p] \leftarrow \{e \in E[p] : i[e] \neq \epsilon\}$
- (3)     **for each**  $(q, w) \in C[p]$
- (4)         do  $E[p] \leftarrow E[p] \cup \{(p, a, w \otimes w', r) : (q, a, w', r) \in E[q], a \neq \epsilon\}$
- (5)         **if**  $q \in F$
- (6)             **then if**  $p \notin F$
- (7)                 **then**  $F \leftarrow F \cup \{p\}$
- (8)                  $\rho[p] \leftarrow \rho[p] \oplus (\omega \oplus \rho[q])$

19. A method of producing an equivalent weighted automaton "B" with no  $\epsilon$ -transitions for any input weighted automaton "A" having a set of transitions E, wherein each transition "e" in the set of transitions has an input label  $i[e]$ , at least one transition being an  $\epsilon$ -transition, a set of states P, each state in the set of states P is denoted as "p", and a set of states Q, each state in the set of states Q denoted as "q", a weight  $w[e]$  for each transition "e", and  $E[p]$  the transitions leaving each state "p" and  $E[q]$  being the transitions leaving state "q", an  $\epsilon$ -closure for a state being defined as  $C[p]$ , and where  $\epsilon[p]$  represents a set of states reachable from state "p" via a path labeled with an  $\epsilon$ -transition, the method comprising:

computing an  $\epsilon$ -closure  $C[p]$  for each state "p" of the input weighted automaton "A";

removing each  $\epsilon$ -transition to produce an automaton  $A_\epsilon$ ; and

adding to  $E[p]$  non-empty-string transitions leaving each state "q" from the set of states reachable from "p" via a path labeled with an  $\epsilon$ -transitions wherein each state "q" is left with its weights pre-multiplied by an  $\epsilon$ -distance from state "p" to "q" in the

automaton "A" to produce the automaton "B" equivalent to automaton A without  $\epsilon$ -transitions.

20. A method of producing an equivalent weighted automaton "B" with no  $\epsilon$ -transitions for any input weighted automaton "A" having a set of transitions " $e$ ", at least one of which is an  $\epsilon$ -transition, a set of states " $p$ ", and a set of states " $q$ ", the method comprising:

computing an  $\epsilon$ -closure  $C[p]$  for each state " $p$ " of the input weighted automaton "A";

for each state " $p$ ", determining the non- $\epsilon$ -transitions from state " $p$ ";

for each state " $q$ " having a weight " $w$ " within the computed  $\epsilon$ -closure  $C[p]$ :

adding to  $E[p]$  the non- $\epsilon$ -transitions leaving each state " $q$ "; and

if state " $q$ " is part of a set of final states  $F$ , and if state " $p$ " is not part of the set of final states  $F$ :

defining state " $p$ " as included within the set of final states " $F$ " and the final weight  $\rho[p]$  as pre- $\otimes$ -multiplied by  $w$ , the  $\epsilon$ -distance from state " $p$ " to state " $q$ " in the automaton A.

21. A method of removing string terms " $a$ " from an automaton A having a set of states " $p$ ", a set of states " $q$ ", and a set of outgoing transitions from the set of states " $p$ ", the method comprising:

computing an  $a$ -closure for each state " $p$ " of the automaton A;

modifying  $E[p]$  by:

removing each transition labeled with a string term " $a$ "; and

adding to  $E[p]$  a non-"a"-string transition, wherein each state "q" is left with its weights pre- $\otimes$ -multiplied by an a-distance from state "p" to a state "q" in the automaton A.

22. The method of claim 21, further comprising:

removing inaccessible states using a depth-first search of the automaton A.

23. The method of claim 21, wherein adding to  $E[p]$  non-"a"-string transitions further comprises leaving q with weights  $(d[p,q] \otimes \rho[q])$  to  $E[p]$ .

24. The method of claim 21, wherein the step of computing an a-closure for each input state of an input automaton A further comprises:

removing all transitions not labeled with a string "a" from automaton A to produce an automaton  $A_a$ ;

decomposing  $A_a$  into its strongly connected components; and

computing all-pairs shortest distances in each component visited in reverse topological order.

25. The method of claim 21, wherein the step of computing an a-closure for each input state of an input automaton A further comprises:

decomposing  $A_a$  into its strongly connected components;

performing a single-source shortest-distance algorithm according to the following pseudo code:

```
1 for each  $p \in Q$ 
2   do  $d[p] \leftarrow r[p] \leftarrow \bar{0}$ 
3   $d[s] \leftarrow r[s] \leftarrow \bar{1}$ 
4   $S \leftarrow \{s\}$ 
```



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5 while S ≠ 0
6   do q ← head [S]
7   DEQUEUE (S)
8   r ← r[q]
9   r[q] ← 0̄
10  for each e ∈ E[q]
11    do if d[n[e]] ≠ d[n[e]] ⊕ (r ⊗ w[e])
12      then d[n[e]] ← d[n[e]] ⊕ (r ⊗ w[e])
13      r[n[e]] ← r[n[e]] ⊕ (r ⊗ w[e])
14      if n[e] ∉ S
15        then ENQUEUE (S, n[e])
16 d[s] ← 1̄

```

26. The method of claim 21, wherein the step of computing the a-closure for each state “p” further comprises computing each of the a-closures according to the following equation:

$$C[p] = \{(q, w) : q \in d[p], d[p, q] = w \in K - \{\bar{0}\}\}.$$

27. The method of claim 26, wherein the step of modifying outgoing transitions of each state “p” further comprises modifying the outgoing transitions of each state p according to the following procedure:

```

(1) for each p ∈ Q
(2)   do E[p] ← {e ∈ E [p] : i[e] ≠ a}
(3)   for each (q, w) ∈ C[p]
(4)     do E[p] ← E[p] ∪ {(p, a, w ⊗ w', r) : (q, a, w', r) ∈ E[q], a ≠ a}
(5)     if q ∈ F
(6)       then if p ∉ F
(7)         then F ← F ∪ {p}
(8)         ρ[p] ← ρ[p] ⊕ (w ⊕ ρ[q])

```

28. The method of claim 27, wherein a state is a final state if some state “q” within a set of states reachable from “p” via a path labeled with an empty string is

final and the final weight is then:  $\rho[p] = \bigoplus_{q \in e[p] \cap F} (d[p, q] \otimes \rho[q])$ .

29. The method of claim 28, further comprising:

performing a depth-first search of the automaton A after removing the "a" strings.

30. A method of removing empty string terms from a transducer A having a set of states "p", a set of states "q", and a set of outgoing transitions from the set of states "p", E[p], the method comprising:

computing an  $\epsilon$ -closure for each state "p" of the transducer A;

modifying E[p] by:

removing each transition labeled with an empty string; and

adding to E[p] a non-empty-string transition, wherein each state "q" is left with its weights pre-multiplied by an  $\epsilon$ -distance from state "p" to a state "q" in the transducer A.

31. The method of claim 30, further comprising:

removing inaccessible states using a depth-first search of the transducer A.

32. The method of claim 30, wherein adding to E[p] non-empty-string transitions further comprises leaving q with weights ( $d[p,q] \otimes \rho[q]$ ) to E[p].

33. The method of claim 30, wherein the step of computing  $\epsilon$ -closure for each input state of an input transducer A further comprises:

removing all transitions not labeled with an empty string from transducer A to produce a transducer  $A_\epsilon$ ;

decomposing  $A_\epsilon$  into its strongly connected components; and

computing all-pairs shortest distances in each component visited in reverse topological order.

34. The method of claim 30, wherein the step of computing  $\varepsilon$ -closure for each input state of an input transducer A further comprises:

decomposing  $A_\varepsilon$  into its strongly connected components;

performing a single-source shortest-distance algorithm according to the following pseudo code:

```
1 for each  $p \in Q$ 
2   do  $d[p] \leftarrow r[p] \leftarrow \bar{0}$ 
3  $d[s] \leftarrow r[s] \leftarrow \bar{1}$ 
4  $S \leftarrow \{s\}$ 
5 while  $S \neq \emptyset$ 
6   do  $q \leftarrow \text{head}[S]$ 
7   DEQUEUE(S)
8    $r \leftarrow r[q]$ 
9    $r[q] \leftarrow \bar{0}$ 
10  for each  $e \in E[q]$ 
11    do if  $d[n[e]] \neq d[n[e]] \oplus (r \otimes w[e])$ 
12      then  $d[n[e]] \leftarrow d[n[e]] \oplus (r \otimes w[e])$ 
13       $r[n[e]] \leftarrow r[n[e]] \oplus (r \otimes w[e])$ 
14      if  $n[e] \notin S$ 
15        then ENQUEUE(S,  $n[e]$ )
16  $d[s] \leftarrow \bar{1}$ 
```

35. The method of claim 30, wherein the step of computing the  $\varepsilon$ -closure for each state "p" further comprises computing each the  $\varepsilon$ -closure according to the following equation:

$$Q[p] = \{(q, w) : q \in \varepsilon[p], d[p, q] = w \in K - \{\bar{0}\}\}.$$

36. The method of claim 35, wherein the step of modifying outgoing transitions of each state "p" further comprises modifying the outgoing transitions of each state p according to the following procedure:

- (1) **for each**  $p \in Q$
- (2)     **do**  $E[p] \leftarrow \{e \in E[p] : i[e] \neq \epsilon\}$
- (3)     **for each**  $(q, w) \in C[p]$
- (4)         **do**  $E[p] \leftarrow E[p] \cup \{(p, a, w \otimes w', r) : (q, a, w', r) \in E[q], a \neq \epsilon\}$
- (5)         **if**  $q \in F$
- (6)             **then if**  $p \notin F$
- (7)                 **then**  $F \leftarrow F \cup \{p\}$
- (8)                  $\rho[p] \leftarrow \rho[p] \oplus (\omega \oplus \rho[q])$

37. The method of claim 36, wherein a state is a final state if some state “q” within a set of states reachable from “p” via a path labeled with an empty string is final and the final weight is then:  $\rho[p] = \bigoplus_{q \in e[p] \cap F} (d[p, q] \otimes \rho[q])$ .

38. The method of claim 37, further comprising:  
performing a depth-first search of the transducer A after removing the empty strings.